

Abstract list functions: Filter, Map

Using `filter`: (`filter even? alist`)

- `filter` consumes a **predicate** specifying which elements of the list are to be **kept**.
- The predicate must be a **one-parameter** function producing a **boolean**, where the type of the parameter is same as the type of the elements of the list

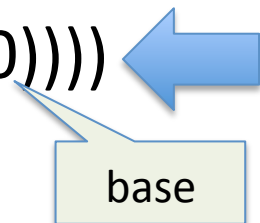
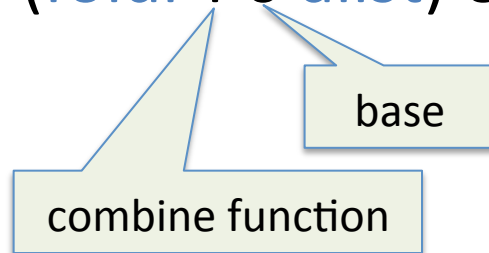
Using `map`: (`map sqr alist`)

- `map` performs the operation of **transforming a list** element-by-element into another list of the **same length**.
- The function consumed by `map` must be a **one-parameter** function where the type of the parameter is the same as the type of the elements of the list.

The abstract list function `foldr`

- `foldr` (built-in) is short for “fold right”.
- It can be viewed as “folding” a list using the provided combine function, starting from the right-hand end of the list.
- If `alist` is `(list x1 x2 . . . xn)`, then by our intuitive explanation of `foldr`, the expression

`(foldr f 0 alist)` equivalent to `(f x1 (f x2 (f ... (f xn 0))))` ←



The abstract list function `foldr` (cont.)

The combine function provided to `foldr` consumes two parameters:

- **an item** in the list that `foldr` consumes and
- the **result** of applying `foldr` to the rest of the list.

Example:

```
(define (f x r)
  (+ x r))

(foldr f 0 (list 1 2 3 4 5))
```

(f 1 (f 2 (f 3 (f 4 (f 5 0))))))



Starting point



base



The abstract list function `foldr` (cont.)

```
(define
  (product-of-numbers alist)
  (cond
    [(empty? alist) 1]
    [else
     (* (first alist) (product-of-
                    numbers (rest alist)))]))
```

- ◆ Similarities
- ◆ Differences

```
(define
  (concat-firsts alist)
  (cond
    [(empty? alist) ""]
    [else
     (cond
      [(string=? "" (first alist))
       (concat-firsts (rest alist))]
      [else (string-append (substring
                            (first alist) 0 1)
                            (concat-firsts (rest alist)))]))]))
```

The abstract list function `foldr` (cont.)

```
(define (foldr combine base alist)
  (cond
    [(empty? alist) base]
    [else (combine (first alist)
                   (foldr combine base (rest alist)))]))
```

Diagram illustrating the function signature and arguments:

- Three blue arrows point upwards from the arguments `combine`, `base`, and `alist` in the function definition to the corresponding arguments in the `cond` branches.
- The first arrow points from `combine` to `(first alist)` in the `else` branch.
- The second arrow points from `base` to `base` in the `else` branch.
- The third arrow points from `alist` to `(rest alist)` in the `else` branch.

Tracing foldr

(foldr f 0 (list 3 6 5))

⇒ (f 3 (foldr f 0 (list 6 5)))

⇒ (f 3 (f 6 (foldr f 0 (list 5))))

⇒ (f 3 (f 6 (f 5 (foldr f 0 empty))))

⇒ (f 3 (f 6 (f 5 0))) ⇒ ...

Intuitively, the effect of the application

(foldr f b (list x_1 x_2 . . . x_n)) is to compute the value of the expression (f x_1 (f x_2 (... (f x_n b) ...))).

Practical Exercise

Write a function *get-total* that produces the total value in a list of numbers.

;; write a function total that produces the sum of the

;; numbers in lon

;; total: (listof Num) -> Num

```
(define (get-total alist)
  (foldr + 0 alist)
)
```



Additional Practical Exercise

Write a function *m-positive* that produces the multiplication of all positive elements of a list of numbers.

```
(define lon (list 1 -2 4 -5 9))
```

```
(define (m-positive lon)  
  (foldr * 1  
    (filter positive? lon)  
    ))
```



Another Practical Exercise

```
(define (f item)
  (or (string? item) (boolean? item)))
```

```
(define (g n)
  (cond [(even? n) (sqr n)] [else (* n 2)]))
```

```
(define (h n s)
  (string-append (substring (number->string n) 0 1) s))
```

- a) `(filter f (list 4 "taco" #\r true "salad" 17 false #\c 8))`
`(list "taco" true "salad" false)`
- b) `(map g (list 4 8 7 1 3))`
`(list 16 64 14 2 6)`
- c) `(foldr h "" (list 16 205 36 5))`
`"1235"`



Using `foldr` to produce lists

- Remember:
 $(\text{foldr } * \ 1 \ \text{alist})$ equivalent to $(* \ x_1 \ (* \ x_2 \ (* \ \dots \ (* \ x_n \ 1) \ \dots)))$
- The functions we provide to `foldr` can also produce cons expressions, since these are also values.
- How? $(\text{cons element-from-list rest-of-list})$
- Example: using `foldr` for `negate-list`.
- `neg-combine` takes the element, negates it, and `conses` it onto the result of the recursive call.

Function `neg-combine`

```
;; neg-combine: Num (listof Num) → (listof Num)
```

```
(define (neg-combine item result-on-rest)  
      (cons (- item) result-on-rest))
```

```
;; negate-list: (listof Num) → (listof Num)
```

```
(define (negate-list alist)  
      (foldr neg-combine empty alist))
```

`foldr` can be used to implement `map`, `filter`, and other abstract list functions.

Boolean functions and `foldr`

`(list 1 2 -3 4) => (list true true false true)`

- `(map positive? (list 1 2 -3 4))`
- To check whether a predicate function produces `true` for every element in a list `alist`, we might be tempted to try:
`(foldr and true (map positive? alist))`
- Problem: `and` is not a function, but a **special form**, and this produces an error.
- Solution: Racket provides `andmap`, which can be used like this: `(andmap positive? alist)`
- For the same reason, `ormap` is provided.

Foldr vs. Template

- Anything that can be done with the **list template** can be done using **foldr**, without explicit recursion.
- Does that mean that the list template is **obsolete**?
- No.
- Experienced Racket programmers still use the list template, for reasons of **readability** and **maintainability**.

Additional Exercise

a. `(define (Z? x)`

`(and (> x 3) (< x 8)))`

`(map sqr (filter Z? (list 5 6 0 -4 12 9 -7))) => (list 25 36)`

b. `(define (f x)`

`(cond [(> x 8) (* x 2)] [else (* x 3)]))`

`(foldr - 1 (map f (list 5 6 1 -4 12 9 -7))) => -4`



c. `(define (w x)`

`(number->string (foldr + 0 x)))`

`(map w (list (list 21 23 30) (list 40 50 60))) => (list "74" "150")`

Another Additional Exercise

Write a function `even-length` that consumes a list of strings, `los`, and produces a list of boolean values where the *i*-th member is `true` if the *i*-th string in `los` is of even length, and `false` otherwise.

For example:

```
(even-length (list "yes" "No" "what" "maybe"))  
=> (list false true true false)
```

For this question you must use only abstract list functions. You may not use explicit recursion.



Another Additional Exercise (cont.)

2. (`define` (`f` `item`)

3. (`even?`

`(string-length item)))`

1. (`map` `f` (`list` `"yes"` `"No"` `"what"` `"maybe"`))

More

We have a the following list of grades:

```
(define grades
```

```
(list (make-grade 'D 62) (make-grade 'C 79) (make-grade 'A 93) (make-  
grade 'B 84) (make-grade 'F 57) (make-grade 'F 38) (make-grade 'A 90)  
(make-grade 'A 95) (make-grade 'C 76) (make-grade 'A 90) (make-grade 'F  
55) (make-grade 'C 74) (make-grade 'A 92) (make-grade 'B 86) (make-  
grade 'F 43) (make-grade 'C 73)))
```

With the following structure defination:

```
;; A Grade is: (make-grade Symbol Number)
```

```
(define-struct grade (letter num)
```



Trying to find the biggest number in this list of grades by using abstract list functions.